

**MATH 217**  
**Exam I**  
**Key**

**1) (21 points)**

a) Stemplot

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1| 1 1 3 4 5 5 6 8 8 9
2| 1 2 3 3 9
3| 0 1 3 8
4| 2 2 5
5| 8
6| 5
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b) The data is highly skewed to the right.

c) We would want to use the 5-Number summary because the mean and standard deviation are not recommended for non-symmetric distributions.

**2) (12 points)**

a) The mean is 27.16 and the median is 22.5.

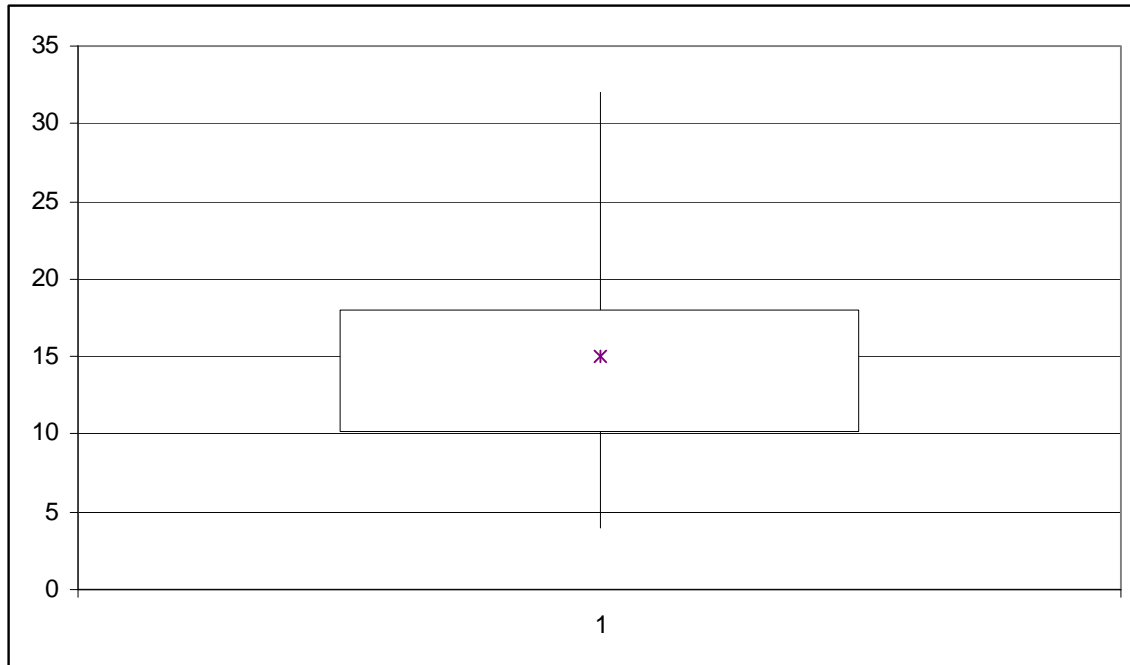
b) The mean is higher than the median. This is not surprising since the distribution is skewed to the right. (*Other answers valid depending on reasoning.*)

**3) (12 points)**

If a distribution is skewed to the left we should expect that the mean will be less than the median as it is pulled to the left.

**4) (12 points)**

The box plot appears below.



To find out if there are any outliers we perform the  $(1.5) \times (IQR)$  test. The interquartile range is  $Q3 - Q1 = 18 - 10 = 8$ . So  $(1.5) \times (IQR) = 1.5 \times 8 = 12$ . Hence, any points falling BELOW  $Q1 - 12 = 10 - 12 = -2$  or ABOVE  $Q3 + 12 = 18 + 12 = 30$  are possible outliers. Since no points fall below  $-2$  there are no lower outliers. However, the maximum value of 32 is greater than 30 implying that 32 could be an outlier.

**5) (18 points)**

Pot-bellied pigs are  $N(90, 6)$ .

- a) To find out the % above 93 we standardize 93 and use the z-table. The z-score for 93 is  $(93 - 90) / 6 = 0.5$ . On the table we see that 0.5 corresponds to 0.6915. Hence, 69.15% of pot-bellied pigs weigh less than 93 lbs, leaving  $100 - 69.15 = 30.75\%$  weigh more.
- b) There are two ways to find the % between 84 and 90. If you noticed that 84 is exactly 1 standard deviation below the mean you can use the 68-95-99.7 rule. This says 68% of the pigs weigh between 84 and 96 lbs. Hence, one half of those lie between 84 and 90. So **34%**. Alternately, you could standardize both scores and get the area between using the z-table.

**6) (10 points)**

The numbers in Table B are all pretty closely clumped around the 20's. In Table A the values range from 10 to 65. **Table A will have the higher standard deviation.**

**7) (15 points)**

- a) The slope of this line is 2. This tells us that the weight of the pig increases for 2 lbs for every additional inch of ear length. (NOTE: We are not talking about increasing the ear length of an individual pig, rather we are talking about comparing multiple pigs with varying ear lengths.)

- b) A pig with 5 inch ears should weigh  $86+2(5)=96$  lbs.
- c) The correlation coefficient being .15 is not good. It tells us that there is a positive relation between pig ear lengths and weight (the longer the ears, the heavier the pig) but the correlation is very low. In general, this equation will not be a good predictor. (Remember, the closer to 0 the closer to NO correlation. We want our correlation coefficient to be reasonably close to +/-1.)

### BONUS

- 1) The pig weighs more than 88% of its fellow pigs. This corresponds to a z-score of approximately 1.18. Hence,  $1.18=[(\text{Pigs Weight})-90]/6$ . Solving this gives the pigs weight as approximately 97.08lbs.
- 2) Standardizing both scores gives you a z-score of  $(78-64)/7=2$  and your friend a z-score of  $(80-71)/7.3=1.23$ . Hence, you were 2 standard deviations above the average and your friend was “only” 1.23 above. You win.

